

- The normals at three points P, Q, R of the parabola  $y^2 = 4ax$  meet in (h, k). The centroid of triangle PQR lies on  
 (a)  $y = 0$  (b)  $x = 0$  (c)  $x = -a$  (d)  $y = a$
- The equation of the tangent at the vertex of the parabola  $x^2 + 4x + 2y = 0$  is  
 (a)  $x = -2$  (b)  $y = 2$  (c)  $x = 2$  (d)  $y = -2$
- The distances from the foci of P  $(x_1, y_1)$  on the ellipse  $\frac{x^2}{9} + \frac{y^2}{25} = 1$  are  
 (a)  $4 \pm \frac{5}{4} y_1$  (b)  $5 \pm \frac{4}{5} y_1$  (c)  $5 \pm \frac{4}{5} x_1$  (d) None of these
- The normal drawn at a point  $(at_1^2, 2at_1)$  of the parabola  $y^2 = 4ax$  meets it again in the point  $(at_2^2, 2at_2)$ , then  
 (a)  $t_1 = 2t_2$  (b)  $t_1^2 = 2t_2$  (c)  $t_1 t_2 = -1$  (d) none of these
- Equation of the normal to the parabola  $y^2 = 4x$  which is parallel to the line  $y = 2x - 5$  is  
 (a)  $y = 2x$  (b)  $y = 2x - 10$  (c)  $y = 2x - 12$  (d) None of these
- The line  $y = mx + 1$  is a tangent to the parabola  $y^2 = 4x$ , is  
 (a)  $m = 2$  (b)  $m = 1$  (c)  $m = 4$  (d)  $m = 3$
- The number of tangents to the parabola  $y^2 = 8x$  through  $(2, 1)$  is  
 (a) 3 (b) 1 (c) 2 (d) 0
- The equation of the hyperbolas having vertices as  $(\pm 5, 0)$ , foci  $(\pm 7, 0)$  is  
 (a)  $24x^2 + 25y^2 = 600$  (b)  $25x^2 - 24y^2 = 600$   
 (c)  $24x^2 - 25y^2 = 600$  (d)  $25x^2 - 24y^2 - 600 = 0$
- The equation of the hyperbola referred to its axes of coordinates whose latus-rectum is 4 and eccentricity is 3 is  
 (a)  $16x^2 + 2y^2 = 1$  (b)  $16^2 - 16y^2 = 1$   
 (c)  $2x^2 - 16y^2 = 1$  (d)  $16x^2 - 2y^2 = 1$
- The eccentricity of the hyperbola whose latus-rectum is 8 and conjugate axis is equal to half the distance between the foci, is  
 (a)  $\frac{4}{5}$  (b)  $\frac{2}{\sqrt{3}}$  (c)  $\frac{4}{\sqrt{3}}$  (d) None of these
- The eccentricity of the hyperbola  $3x^2 - 4y^2 = -12$  is  
 (a)  $-\sqrt{\frac{7}{3}}$  (b)  $\frac{\sqrt{7}}{2}$  (c)  $\sqrt{\frac{7}{3}}$  (d)  $-\frac{\sqrt{7}}{2}$
- If  $e_1$  and  $e_2$  are the eccentricities of a hyperbola and its conjugate hyperbola, then  $1/e_1^2 =$   
 (a)  $1 - 1/e_2^2$  (b)  $1 + 1/e_1^2$  (c)  $1/e_2^2 - 1$  (d) None of these
- Equation of the tangent to the hyperbola  $2x^2 - 3y^2 = 6$  which is parallel to the line  $y = 3x + 4$  is  
 (a)  $y = 3x + 5$  (b)  $y = 3x - 5$   
 (c) both (a) and (b) (d) None of these
- The locus of the mid-point of a focal chord of a parabola is  
 (a) circle (b) parabola (c) ellipse (d) hyperbola
- The line  $x + y = 6$  is a normal to the parabola.  $y^2 = 8x$  at the point  
 (a)  $(18, -12)$  (b)  $(4, 2)$  (c)  $(2, 4)$  (d)  $(3, 3)$

16. The straight line  $x + y = k + 1$  touches the parabola  $y = x(1 - x)$  if  
 (a)  $k = -1$  (b)  $k = 0$  (c)  $k = 1$  (d)  $k$  takes any value
17. The locus of the point of intersection of the tangents to the ellipse  $x^2/a^2 + y^2/b^2 = 1$  which are at right angles is  
 (a) a circle (b) parabola (c) an ellipse (d) a hyperbola
18. If the line  $y = mx + a$  meets the parabola  $y^2 = 4ax$  in two points whose abscissa are  $x_1$  and  $x_2$ , then  $x_1 + x_2$  is equal to zero if  
 (a)  $m = -1$  (b)  $m = 1$  (c)  $m = 2$  (d)  $m = -1/2$
19. If P, Q, R are three points on a parabola  $y^2 = 4ax$  whose ordinates are in geometrical progression, then the tangents at P and R meet on  
 (a) the line through Q parallel to x-axis (b) the line through Q parallel to y-axis  
 (c) the line joining Q to the vertex (d) the line joining Q to the focus
20. The tangents at three points A, B, C on the parabola  $y^2 = 4ax$ , taken in pairs intersect at the points P, Q and R. If  $\Delta, \Delta'$  be the areas of the triangles ABC and PQR respectively, then  
 (a)  $\Delta = 2\Delta'$  (b)  $\Delta' = 2\Delta$  (c)  $\Delta = \Delta'$  (d) none of these
21. An arc of a bridge is semi-elliptical with major axis horizontal. If the length of the base is 9 meter and the highest part of the bridge is 3 meter from the horizontal; the best approximation of the height of the arch 2 meter from the centre of the base is  
 (a)  $11/4$  m (b)  $8/3$  m (c)  $7/2$  m (d) 2 m
22. Sum of the focal distances of any point on the ellipse  $x^2/a^2 + y^2/b^2 = 1$  is equal to the length of the  
 (a) major axis (b) minor axis (c) latus rectum (d) none of these
23. Two tangents are drawn from the pt.  $(-2, -1)$  to the parabola  $y^2 = 4x$ . If  $\alpha$  is the angle between these tangents, then  $\tan \alpha =$   
 (a) 3 (b)  $1/3$  (c) 2 (d)  $1/2$
24. The graph represented by the equations  $x = \sin^2 t, y = 2 \cos t$  is  
 (a) a portion of a parabola (b) a parabola  
 (c) a part of a sine graph (d) a part of a hyperbola
25. The tangents at the points  $(at_1^2, 2at_1), (at_2^2, 2at_2)$  on the parabola  $y^2 = 4ax$  are at right angle if  
 (a)  $t_1 t_2 = -1$  (b)  $t_1 t_2 = 1$  (c)  $t_1 t_2 = 2$  (d)  $t_1 t_2 = -2$
26. The vertex of the parabola  $x^2 + 8x + 12y + 4 = 0$  is  
 (a)  $(-4, 1)$  (b)  $(4, -1)$  (c)  $(-4, -1)$  (d)  $(4, 1)$
27. The focus of the parabola  $y^2 - 4y - 8x + 4 = 0$  is  
 (a)  $(1, 1)$  (b)  $(1, 2)$  (c)  $(2, 1)$  (d)  $(2, 2)$
28. At what point on the parabola  $y^2 = 4x$  the normal makes equal angles with the axes?  
 (a)  $(4, 4)$  (b)  $(9, 6)$  (c)  $(4, -4)$  (d)  $(1, -2)$
29. If  $x = my + c$  is a normal to the parabola  $x^2 = 4ay$ , then the value of  $c$  is  
 (a)  $-2am - am^3$  (b)  $2am + am^3$  (c)  $-\frac{2a}{m} - \frac{a}{m^3}$  (d)  $\frac{2a}{m} + \frac{a}{m^3}$
30. The angle between the tangents drawn from a point  $(-a, 2a)$  to  $y^2 = 4ax$  is  
 (a)  $\frac{\pi}{4}$  (b)  $\frac{\pi}{2}$  (c)  $\frac{\pi}{3}$  (d)  $\frac{\pi}{6}$